# Fed-EE: Federating Heterogeneous ASR Models using Early-Exit Architectures

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# Abstract

Automatic speech recognition models require large speech recordings for training. 1 2 However, the collection of such data often is cumbersome and leads to privacy concerns. Federated learning has been widely used as an effective decentralized 3 4 technique that collaboratively learns a shared model while keeping the data local on clients devices. Unfortunately, client devices often feature limited computation 5 and communication resources leading to practical difficulties for large models. 6 In addition, the heterogeneity that characterizes edge devices make unpractical 7 federating a single model that fits all the different clients. Differently from the 8 recent literature, where multiple different architectures are used, in this work we 9 propose using early-exiting. This brings 2 benefits: a single model is used on a 10 variety of devices; federating the models is straightforward. Experiments on the 11 public dataset TED-LIUM 3 show that our proposed approach is effective and can 12 be combined with basic federated learning strategies. We also shed light on how 13 14 to federate self-attention models for speech recognition, for which an established 15 recipe does not exist in literature.

# **16 1 Introduction**

<sup>17</sup> D eep learning-based approaches are now widely employed for automatic speech <sup>18</sup> D recognition (ASR) [20], mainly using large centralized training sets [28, 1, 18].

Unfortunately, centralized training 19 poses issues related to data ownership, 20 data privacy, latency, and cost; these 21 aspects gained increasing attention 22 with the proliferation of both edge 23 devices and low-latency communica-24 tion technologies [17]. Therefore, dis-25 26 tributed training approaches, such as federated learning (FL), have recently 27 received more spotlight [5, 9]. As de-28 picted in Fig. 1(a), FL is a distributed 29 30 machine learning approach that aims to train models by combining pieces 31

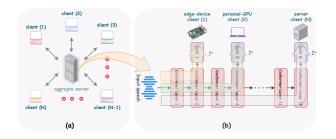


Figure 1: (a) FL scenario. (b) Example of EE architectures: different clients accommodate different exits.

of information collected on the edge
devices [23]. In details, in each FL round a set of clients performs local training using the locally
acquired data and share with the central server the information needed to update the central models
(e.g. gradients, weights, etc.). The server agglomerates the received updates and sends the models
back to the clients to perform their processing. In this way, most of the computation is executed on
the edge, preserving at the same time, private data to be transmitted over communication networks.

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In a distributed environment edge devices exhibit a large variability of computational assets demanding 38 for resource aware, i.e. client specific, neural networks. This issue can be handled by employing 39 different architectures, with different resource requirements, and federating them via some shared 40 layer or common processing blocks, as proposed in [49, 36, 4], eventually implementing articulated 41 agglomeration strategies. Instead, in this work we propose to use early-exit (EE) architectures, that 42 decode the outputs at different layers of an encoder, as depicted in Fig. 1(b). In this way, a single EE 43 model is managed at the server side, while only the layers fitting the resources available on clients are 44 actually processed locally. In particular, with this work we aim to contribute to the scientific literature 45 in the three directions. 1) We show that EE models allow federating heterogeneous models in a rather 46 straightforward way. This surpasses the need for multiple models centrally aligned with edge-specific 47 solutions of current approaches, as in [5]. 2) The literature on FL for ASR is not uniform in relation 48 to model pretraining and centralized training on held-out data [9, 32]. We experimentally confirm that 49 in a cross-domain framework, pretraining even on out-of-domain data is indeed necessary, but the 50 role of central training seems not to be crucial. 3) We show that using the FedAdam agglomeration 51 strategy [39] in combination with freezing part of the pretrained model (pretrained in an EE fashion) 52 noticeably helps the convergence. Note that although FedAdam has been already used in literature, 53 its efficacy on ASR tasks with EE architectures has never been experimentally verified. 54

#### **Related Works** 2 55

In speech processing, federated learning has been applied to several tasks: ASR [13, 46], keyword 56 spotting [22, 27, 14], speaker recognition [45] and other applications [21, 10, 8]. Generally, FL for 57 ASR is a challenging task. Other than for the classic non-i.i.d and unbalancing data distributions, the 58 main critical issues are: a) most of ASR architectures (e.g Transformers [48], Transducers [30, 47] 59 and recurrent neural networks [34]) require powerful computational resources which are not available 60 in most edge devices, and b) learning, from scratch, the proper alignment between the latent speech 61 representation and the transcription [40] is unfeasible in a FL framework, since it requires large 62 datasets, usually available only in the central servers. In [9], the authors prove the need to pretrain 63 the global model in order to reach convergence and introduce a held-out data set, to be employed 64 after FedAvg, to control model divergence between adjacent FL rounds. They also apply some 65 (client-specific) weighting strategies in FedAvg agglomeration, showing the superior performance of 66 word error rate (WER)-based weighting compared to loss-based weighting. Similar trends of results 67 have been observed on LibriSpeech [35], as reported in [6]. [32] investigated the use of a global 68 69 model initialized as in [9] or based on a pretrained self-supervised model (Wav2Vec 2.0 [2]), using 70 FL to adapt to the TEDLIUM-3 dataset [15]. While FL did not improve the WER of the former model, the latter has demonstrated effective. In the following, we show that our proposed EE model 71 allows applying FL on TEDLIUM-3 without the need of a large self-supervised pretrained model 72 (pretraining is on LibriSpeech). 73

#### 2.1 Federated learning for Heterogeneous models 74

75 Most FL approaches assume that all clients are "homogeneous" in their computational assets. However, this hypothesis cannot be applied in real scenarios, where devices may have severe limitations 76 in their memory, computation capabilities, and power consumption and are characterized by a 77 dynamic usage of the resources. Therefore, FL frameworks require managing multiple different 78 "heterogeneous" architectures, under the guidance of personalized tasks and local resource constricts 79 [42]. 80

81 Previous works have addressed the client heterogeneity by employing multiple different architectures all sharing a common part. In particular: a) mixed model architectures [29], where local models 82 share only a subset of parameters with the central model, b) knowledge distillation [33, 26] at the 83 client side to preserve the global model parameters while learning local information, c) the usage of a 84 contrastive loss [25] to decrease a distance metric between central and local models, and d) federated 85 ensemble knowledge transfer (Fed-ET) [5], that uses a consensus distillation, derived from clients, to 86 train a large model on the server (also in this case networks share some common layers). 87 With respect to the previous works, we propose using EE architectures that introduce intermediate 88

exit branches [43, 37] to the network (see Fig. 1(b)): the input is processed by a subset of the layers 89 of the neural network, resulting in multiple scaled versions of the same architectures. In section 3.1 90 we show that the EE architecture allows to agglomerate coherently the local model parameters at 91 the server side and to further extract from the global model the suitable sub-models to be sent to the 92

connected clients. 93

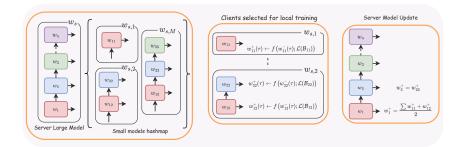


Figure 2: Illustration of our proposed approach for agglomerating heterogeneous models.

# 94 **3** Proposed Approach

The idea of FL is to train multiple versions of a neural model on the client side and then agglomerate 95 them on the server side. Let us assume that C clients are available at round  $\tau$ , and each client 96  $c \in \{1, ..., C\}$  observes its own training set  $\mathcal{B}_c$ . At the beginning of each round, clients receive 97 the most recently trained model stored on the central server  $\mathbf{w}_c^-(\tau) = \mathbf{w}_s(\tau-1)$ . Note that an 98 important requirement here is that all clients can accommodate the same architecture. Each model is 99 updated using the local dataset  $\mathbf{w}_{c}^{+}(\tau) \leftarrow f(\mathbf{w}_{c}^{-}(\tau); \mathcal{L}(\mathcal{B}_{c}))$ , where  $\mathcal{L}(\mathcal{B}_{c})$  is the loss computed on 100 the dataset of client c and  $f(\cdot)$  is a weight update strategy (i.e. SGD, ADAM, etc.). Local models are 101 in turn used to update the central model  $\mathbf{w}_s(\tau)$ . 102

Recently, several works have been published to find the optimal strategy to agglomerate clients' model parameters (weights) [5, 38, 31] or to improve the type and amount of information shared between the clients and the server [24]. Federated averaging strategy (FedAvg) [19], which is based on FedSGD [7], is one of the most common strategies as it agglomerates the models by simple weighted averaging:  $\mathbf{w}_s(\tau) = \frac{1}{C} \sum_{c=1}^{C} \eta_c(\tau) \mathbf{w}_c^+(\tau)$ , where the weights  $\eta_c(\tau)$  (such that  $\sum_{c=1}^{C} \eta_c(\tau) = 1$ ) are estimates of the client confidence, eventually related to the size of the dataset  $\mathcal{B}_c$ , the loss  $\mathcal{L}(\mathcal{B}_c)$ or the accuracy on a local or centralized development set.

One of the limitations of FedAvg is the need to use SGD on the clients in order to allow an effective averaging of the different models, affecting the overall convergence. FedAdam [39] is an alternative

agglomeration strategy that updates the weights using one-step adaptive gradient optimization [44].

# 113 3.1 Federated Learning with Early-Exit models

In the presence of devices with different processing capabilities, using a single model  $\mathbf{w}$  is not feasible. As mentioned above, current approaches employ U different networks  $\mathbf{w}^u$ , u = [1, ..., U] with different computation requirements which are all maintained on the centralized server. This solution requires managing multiple different models, with varying performance, and adopting articulated strategies for agglomerating them.

As mentioned in section 2.1 an interesting solution is offered by EE architectures. Let us assume that model  $\mathbf{w}_s$  is split in M subnets  $\mathbf{w}_{s,1}, \mathbf{w}_{s,2}, \ldots, \mathbf{w}_{s,M}$  (not necessarily of the same type) each of them equipped with an exit layer (producing hypothesis  $\hat{\mathbf{y}}^1, \ldots, \hat{\mathbf{y}}^M$ ). The overall model is trained by optimizing the joint objective  $\mathcal{L}_{EE}(\hat{\mathbf{y}}^1, \ldots, \hat{\mathbf{y}}^M, \mathbf{y}) = \sum_m \mathcal{L}(\hat{\mathbf{y}}^m, \mathbf{y}) = \sum_m \mathcal{L}_m(\mathcal{B})$ , where  $\mathcal{L}(\hat{\mathbf{y}}^m, \mathbf{y})$  and  $\mathbf{y}^m$  are the loss and the prediction of the *m*-th, while  $\mathbf{y}$  is the ground-truth label.

It is worth noting that besides reducing the actual number of models, EE allows applying standard 124 agglomeration strategies such as FedAvg and FedAdam. More in detail, each client c is equipped 125 with a model  $\mathbf{w}_{c,i}$ , which includes all sub-nets up to  $i \in [1, M]$ . According to the notation above 126 the weight updates are done as  $\mathbf{w}_{c,i}^+(\tau) \leftarrow f\left(\mathbf{w}_{c,i}^-(\tau); \sum_{m=1}^i \mathcal{L}_m(\mathcal{B}_c)\right)$ . Then the updated local 127 weights are sent to the server where they are averaged according to all sub-nets. Fig.2 shows the 128 graphical representation of the proposed approach in the case of only two clients. Note that while the 129 subnet  $\mathbf{w}_{s,1}$  is present in all clients, higher subnets ( $\mathbf{w}_{s,M}$ ) are less frequent and may be not updated. 130 Nevertheless, if  $C \gg M$  it is likely that all subnets are present in some clients. 131

Table 1: WER of the model pretrained on Librispeech and TEDLIUM-3 tested on both Librispeech
and TEDLIUM-3. The third column reports the heterogeneous FL performance using FedAdam and
freezing the convolutional layers.

Train set	Librispeech-960		FedAdam - Hetero -freeze	TED-LIUM
Test set	Libri-Test-Clean	TED-LIUM-Test	TED-LIUM-Test @ 1400 rounds	TED-LIUM-Test (upper-bound)
exit 1	24.10	50.94	45.40	43.8
exit 2	11.78	34.50	29.93	23.4
exit 3	6.91	29.58	24.31	18.0
exit 4	6.28	28.61	2343	16.1
exit 5	7.30	28.79	23.36	14.9
exit 6	5.34	27.35	21.83	14.6

# **132 4 Experimental Setup**

We evaluate our proposed approach using the TEDLIUM-3 corpus [15] that contains TED talks with 133 a total amount of 452 hours of speech data in English from about 2351 speakers. As previously 134 mentioned and as observed in previous studies [32], training an ASR model from scratch in a federated 135 fashion is unfeasible. Therefore, we pretrain our model using the whole training set (960 hours) 136 of Librispeech. Following the best practice in literature and in an attempt to make the scenario as 137 realistic as possible, the TEDLIUM training set is split such that each client sees data of a single 138 speaker (this way mimicking personal devices). Performance is measured in terms of WER on the 139 test set for each of the M exits of the resulting agglomerated model. Note that, differently from the 140 current literature, we adapt the initial model, trained on LibriSpeech, to a new domain ("TEDLIUM"), 141 instead of applying FL to the same domain ("LibriSpeech"). For ASR, we use the EE architecture 142 depicted in Fig. 1(b): it consists of a stack of conformer layers with intermediate linear decoders 143 every other conformer.<sup>2</sup> Further details are given in Sec. A.1. 144

We implement the FL framework using the Flower toolkit [3]. We deploy 2351 clients (one for each 145 speaker in the training set). In each round, 10% of all available clients are randomly instantiated 146 and used to train the model locally. Local training implements SGD for 5 epochs using a learning 147 rate equal to 0.01. Models are centrally agglomerated using either FedAvg or FedAdam. Finally, we 148 consider a classic scenario where homogeneous models are used (i.e. the full early-exit architecture) 149 as well as the case where models are *heterogeneous*. In the latter, the number of exits available at 150 each client randomly varies across clients and rounds with a uniform probability distribution. Finally, 151 in order to improve the model convergence, we also experiment with freezing the convolutional front 152 end of the pretrained model, training only the encoder-decoder part. Our code is publicly available<sup>3</sup>. 153

# 154 4.1 Experimental Results

Table 1 reports the performance of our approach considering heterogeneous architectures. The first 155 column reports the performance of our model pretrained and tested on Librispeech confirming that it is 156 a solid baseline. The second column reports the performance of the pretrained model on TEDLIUM-3: 157 this is the starting point for our FL experiment. The third column reports the WER obtained with 158 1400 FL rounds using heterogeneous architectures with FedAdam and freezing the feature extractor, 159 while the last column reports the upper-bound on TEDLIUM-3 when applying central training. The 160 first interesting result is that even if heterogeneous devices are used (i.e. the whole architecture is not 161 available at all clients) agglomerating the models with a standard FL approach is viable: note that 162 WERs are considerably better than those of the initial model at all exits. 163

Fig. 3 compares the WER obtained with heterogeneous and homogeneous architectures as a function of the FL rounds for 3 exits: 1,3 and 6. Note that the performance in both cases are very similar using either FedAvg (lines orange and black) or FedAdam (lines green and red) for all exits. This further confirms the efficacy of EE models in this scenario. The figure also confirms that both FedAdam and freezing the convolutional layers noticeably speed up the convergence of the model with respect to FedAvg. As a matter of fact, the convolutional front-end is in charge of extracting robust features for speech recognition, so it makes sense that it does not need to be adapted to a new speech domain.

<sup>&</sup>lt;sup>2</sup>https://github.com/augustgw/early-exit-transformer

<sup>&</sup>lt;sup>3</sup>https://github.com/mnabihali/ASR-FL

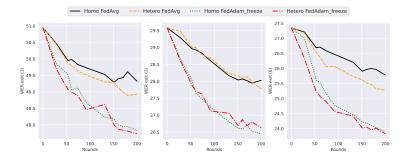


Figure 3: WER achieved with homogeneous and heterogeneous models, using FedAvg and FedAdam with freezing the convolutional front-end. Three different exits are reported.

## 171 **5** Conclusions

In this paper, we have presented an investigation on FL for ASR in the presence of heterogeneous clients using early-exit architectures. The experimental results obtained on popular benchmarks proved the efficacy of the EE models in this scenario. Differently from other works in the literature, we employ a pre trained EE model from out-of-domain data. We demonstrate that centralized training is not crucial for model convergence. Finally, we observed significant performance improvements when freezing the convolutional layers of the pretrained model.

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# **282** A Supplementary Material

### 283 A.1 ASR model

For the ASR model, we use the early-exit architecture shown in Fig. 1(b). The network takes as input 80 Mel Frequency Cepstral Coefficients (MFCCs). This MFCC sequence is passed through a series of a stack of N = 12 conformer layers with M = 6 intermediate linear decoders (one every 2 conformer layers,  $M = \frac{N}{2}$ ). The optimal sequence of labels in each decoder is chosen by means of the CTC algorithm [11, 12]. The model uses a byte pair encoding (BPE) based tokenizer [41] with 256 tokens. Table 2 summarizes the main hyperparameters for the model.

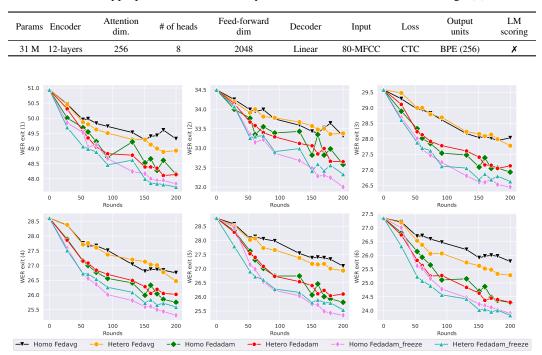


Table 2: Hyperparameters for the early-exit model architecture shown in Fig.1(b).

Figure 4: WER achieved by different FL strategies on TEDLIUM 3. The figure shows results with homogeneous and heterogeneous models, using FedAvg and FedAdam, as well as freezing the convolutional front-end.

### 290 A.2 Further experimental results

Figure 4 complements the results reported above with the performance of FedAdam without freezing and considering all the exits. Note that both FedAdam and freezing the convolutional layers contribute to improving the convergence of the model.

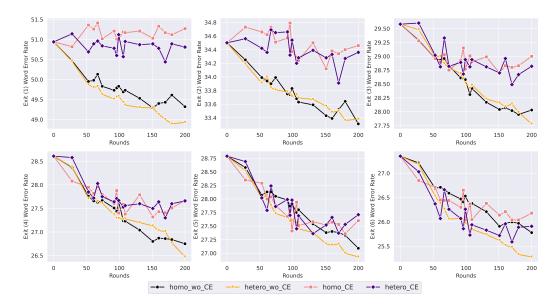


Figure 5: WER using FedAvg strategy with and without a central training stage.

# 294 A.3 On the use of central training

We also experiment with centrally training the agglomerated model using the TEDLIUM 3 devel-295 opment set. This is a common practice in literature when a pretrained model is available and FL 296 is applied on data from the same domain [9, 16]. Typically a part of the training set is held out for 297 the central training whose main role is to avoid the model diverges. In our scenario, we used the 298 development set of TEDLIUM-3 as central training: it includes 8 speakers for a total of 1.6 hours. 299 After agglomerating the local models we run 15 epochs of SGD on the development set. Fig. 5 shows 300 the results. Note that for the last two exits the use of central training does not bring any improvement 301 over a basic FedAvg method. Interestingly, for earlier exits the use of a small set for central training 302 is instead detrimental. The reason behind this behavior is that, the TEDLIUM-3 development set 303 has not enough samples to train the server large model. Hence, the server model tends to overfit the 304 development set. 305